

Chapter 4 Complex Numbers

Section 4.1 Complex Numbers

Objective: In this lesson you learned how to perform operations with complex numbers.

Course Number

Instructor

Date

Important Vocabulary

Define each term or concept.

Complex numbers

Complex conjugates

I. The Imaginary Unit i (Page 310)

Mathematicians created an expanded system of numbers using the **imaginary unit i** , defined as $i = \underline{\hspace{2cm}}$, because . . .

What you should learn

How to use the imaginary unit i to write complex numbers

By definition, $i^2 = \underline{\hspace{2cm}}$.

Each complex number can be written in the **standard form** $\underline{\hspace{2cm}}$, where the number $\underline{\hspace{2cm}}$ is called the **real part** of the complex number, and the number $\underline{\hspace{2cm}}$ is called the **imaginary part** of the complex number.

For the complex number $a + bi$, if $b = 0$, the number $a + bi = a$ is a(n) $\underline{\hspace{2cm}}$. If $b \neq 0$, the number $a + bi$ is a(n) $\underline{\hspace{2cm}}$. If $a = 0$, the number $a + bi = bi$ is a(n) $\underline{\hspace{2cm}}$.

The set of complex numbers consists of the set of $\underline{\hspace{2cm}}$ and the set of $\underline{\hspace{2cm}}$.

Two complex numbers $a + bi$ and $c + di$, written in standard form, are equal to each other if . . .

II. Operations with Complex Numbers (Pages 311–312)

To add two complex numbers, . . .

What you should learn
How to add, subtract, and multiply complex numbers

To subtract two complex numbers, . . .

The **additive identity** in the complex number system is _____.

The **additive inverse** of the complex number $a + bi$ is

_____.

Example 1: Perform the operations:

$$(5 - 6i) - (3 - 2i) + 4i$$

To multiply two complex numbers $a + bi$ and $c + di$, . . .

Example 2: Multiply: $(5 - 6i)(3 - 2i)$

III. Complex Conjugates and Division (Page 313)

The product of a pair of complex conjugates is a(n)

_____ number.

What you should learn
How to use complex conjugates to divide complex numbers

To find the quotient of the complex numbers $a + bi$ and $c + di$, where c and d are not both zero, . . .

Example 3: Divide $(1 + i)$ by $(2 - i)$. Write the result in standard form.

IV. Complex Solutions of Quadratic Equations (Page 314)

If a is a positive number, the **principal square root** of the negative number $-a$ is defined as _____.

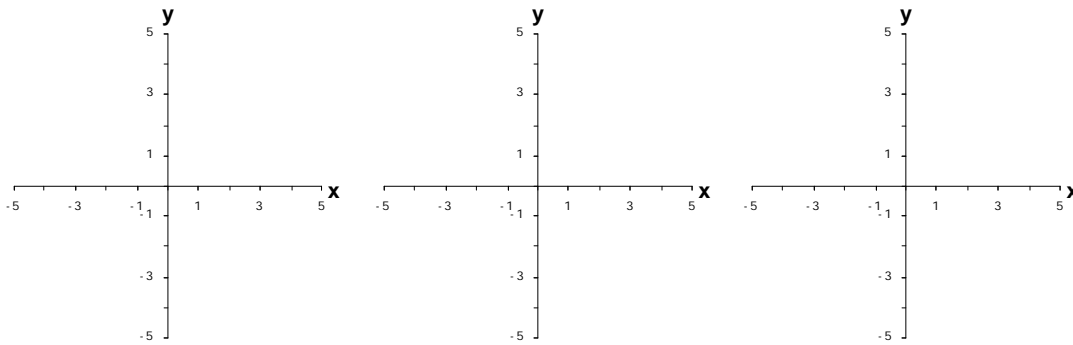
To avoid problems with multiplying square roots of negative numbers, be sure to convert to _____ before multiplying.

Example 4: Perform the operation and write the result in standard form: $(5 - \sqrt{-4})^2$

Example 5: Find the solutions of the quadratic equation $4x^2 - 4x + 5 = 0$.

What you should learn
How to use the Quadratic Formula to find complex solutions of quadratic equations

Additional notes

Additional notes**Homework Assignment**

Page(s)

Exercises