

## Section 2.2 Polynomial Functions of Higher Degree

**Objective:** In this lesson you learned how to sketch and analyze graphs of polynomial functions.

Course Number

Instructor

Date

### Important Vocabulary

Define each term or concept.

**Continuous**

**Extrema**

**Relative minimum**

**Relative maximum**

**Repeated zero**

**Multiplicity**

**Intermediate Value Theorem**

### I. Graphs of Polynomial Functions (Pages 103–104)

Name two basic features of the graphs of polynomial functions.

- 1)
- 2)

Will the graph of  $g(x) = x^7$  look more like the graph of  $f(x) = x^2$  or the graph of  $f(x) = x^3$ ? Explain.

#### *What you should learn*

How to use transformations to sketch graphs of polynomial functions

### II. The Leading Coefficient Test (Pages 105–106)

State the **Leading Coefficient Test**.

1.
  - a.
  - b.
2.
  - a.
  - b.

#### *What you should learn*

How to use the Leading Coefficient Test to determine the end behavior of graphs of polynomial functions

**Example 1:** Describe the left and right behavior of the graph of  
 $f(x) = 1 - 3x^2 - 4x^6$ .

### III. Zeros of Polynomial Functions (Pages 106–110)

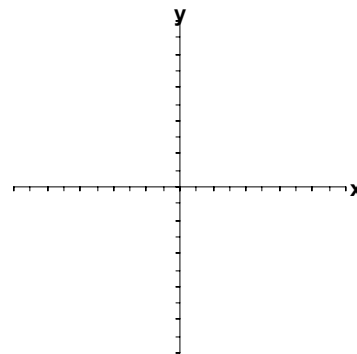
Let  $f$  be a polynomial function of degree  $n$ . The function  $f$  has at most \_\_\_\_\_ real zeros. The graph of  $f$  has at most \_\_\_\_\_ relative extrema.

**What you should learn**  
 How to find and use zeros of polynomial functions as sketching aids

Let  $f$  be a polynomial function and let  $a$  be a real number. List four equivalent statements about the real zeros of  $f$ .

- 1)
- 2)
- 3)
- 4)

If a polynomial function  $f$  has a repeated zero  $x = 3$  with multiplicity 4, the graph of  $f$  \_\_\_\_\_ the  $x$ -axis at  $x =$  \_\_\_\_\_. If  $f$  has a repeated zero  $x = 4$  with multiplicity 3, the graph of  $f$  \_\_\_\_\_ the  $x$ -axis at  $x =$  \_\_\_\_\_.



**Example 2:** Sketch the graph of  $f(x) = \frac{1}{4}x^4 - 2x^2 + 3$ .

### IV. The Intermediate Value Theorem (Pages 111)

Interpret the meaning of the Intermediate Value Theorem.

**What you should learn**  
 How to use the Intermediate Value Theorem to help locate zeros of polynomial functions

Describe how the Intermediate Value Theorem can help in locating the real zeros of a polynomial function  $f$ .

#### Homework Assignment

Page(s)

Exercises