

Section 11.4 Limits at Infinity and Limits of Sequences

Objective: In this lesson you learned how to evaluate limits at infinity and find limits of sequences.

Course Number

Instructor

Date

I. Limits at Infinity and Horizontal Asymptotes

(Pages 811–814)

Define **limits at infinity**.

What you should learn
How to evaluate limits of functions at infinity

To help evaluate limits at infinity, you can use the following:

If r is a positive real number, then $\lim_{x \rightarrow \infty} \frac{1}{x^r} = \underline{\hspace{2cm}}$.

If x^r is defined when $x < 0$, then $\lim_{x \rightarrow -\infty} \frac{1}{x^r} = \underline{\hspace{2cm}}$.

Example 1: Find the limit: $\lim_{x \rightarrow \infty} \frac{1 + 5x - 3x^3}{x^3}$

If $f(x)$ is a rational function and the limit of f is taken as x approaches ∞ or $-\infty$,

- When the degree of the numerator is less than the degree of the denominator, the limit is $\underline{\hspace{2cm}}$.
- When the degrees of the numerator and the denominator are equal, the limit is $\underline{\hspace{2cm}}$.
- When the degree of the numerator is greater than the degree of the denominator, the limit $\underline{\hspace{2cm}}$.

II. Limits of Sequences (Pages 815–816)

For a sequence whose n th term is a_n , as n increases without bound, if the terms of the sequence get closer and closer to a particular value L , then the sequence is said to

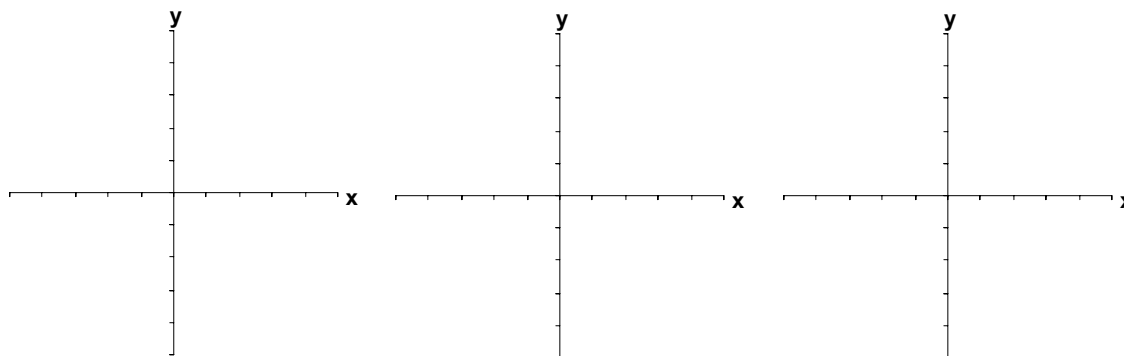
_____ to L . Otherwise, a sequence that does not converge is said to _____.

Give the definition of the limit of a sequence.

What you should learn

How to find limits of sequences

Example 2: Find the limit of the sequence $a_n = \frac{(n-3)(4n-1)}{4-3n-n^2}$.

**Homework Assignment**

Page(s)

Exercises