

Section 10.2 Vectors in Space

Objective: In this lesson you learned how to represent vectors and find dot products of and angles between vectors in space.

Course Number

Instructor

Date

Important Vocabulary

Define each term or concept.

Standard unit vector notation in space**Angle between two nonzero vectors in space****Parallel vectors in space****I. Vectors in Space** (Pages 750–752)

In space, vectors are denoted by ordered triples of the form

_____.

The **zero vector in space** is denoted by _____.

If \mathbf{v} is represented by the directed line segment from $P(p_1, p_2, p_3)$ to $Q(q_1, q_2, q_3)$, the **component form** of \mathbf{v} is produced by . . .

What you should learn

How to find the component forms of, the unit vectors in the same direction of, the magnitudes of, the dot products of, and the angles between vectors in space

Two vectors are **equal** if and only if . . .

The **magnitude**(or length) of $\mathbf{u} = \langle u_1, u_2, u_3 \rangle$ is:

$$\|\mathbf{u}\| = \sqrt{\frac{\quad}{\quad}}$$

A unit vector \mathbf{u} in the direction of \mathbf{v} is _____.

The **sum** of $\mathbf{u} = \langle u_1, u_2, u_3 \rangle$ and $\mathbf{v} = \langle v_1, v_2, v_3 \rangle$ is

$$\mathbf{u} + \mathbf{v} = \frac{\quad}{\quad}$$

The **scalar multiple** of the real number c and $\mathbf{u} = \langle u_1, u_2, u_3 \rangle$ is

$$c\mathbf{u} = \underline{\hspace{2cm}}.$$

The **dot product** of $\mathbf{u} = \langle u_1, u_2, u_3 \rangle$ and $\mathbf{v} = \langle v_1, v_2, v_3 \rangle$ is

$$\mathbf{u} \cdot \mathbf{v} = \underline{\hspace{2cm}}$$

If θ is the angle between two nonzero vectors \mathbf{u} and \mathbf{v} , then

$$\cos \theta = \underline{\hspace{2cm}}.$$

If the dot product of two nonzero vectors is zero, the angle between the vectors is . Such vectors are called .

Example 1: Find the dot product of the vectors $\langle -1, 4, -2 \rangle$ and $\langle 0, -1, 5 \rangle$.

II. Parallel Vectors (Pages 752–753)

Example 2: Determine whether the vectors $\langle 6, 1, -3 \rangle$ and $\langle -2, -1/3, 1 \rangle$ are parallel.

What you should learn
How to determine whether vectors in space are parallel or orthogonal

To use vectors to determine whether three points P , Q , and R in space are collinear, . . .

III. Applications of Vectors in Space (Page 754)

Describe a real-life application of vectors in space.

What you should learn
How to use vectors in space to solve real-life problems

Homework Assignment

Page(s)

Exercises