

## Section 7.3 Multivariable Linear Systems

**Objective:** In this lesson you learned how to solve a system of equations by Gaussian elimination, how to recognize linear systems in row-echelon form and to use back substitution to solve the system, how to solve nonsquare systems of equations, and how to use a system of equations to model and solve real-life problems.

Course Number

Instructor

Date

### Important Vocabulary

Define each term or concept.

**Row-echelon form**

**Ordered triple**

**Gaussian elimination**

**Nonsquare system of equations**

**Three-dimensional coordinate system**

**Graph of an equation in three variables**

**Partial fraction**

**Partial fraction decomposition**

**Basic equation**

### I. Row-Echelon Form and Back-Substitution (Page 509)

When elimination is used to solve a system of linear equations, the goal is . . .

#### *What you should learn*

How to recognize linear systems in row-echelon form and use back-substitution to solve the systems

**Example 1:** Solve the system of linear equations.

$$\begin{cases} x + y - z = 9 \\ y - 2z = 4 \\ z = 1 \end{cases}$$

**II. Gaussian Elimination** (Pages 510–512)

To solve a system that is not in row-echelon form, . . .

***What you should learn***  
How to use Gaussian elimination to solve systems of linear equations

List the three elementary row operations that can be used on a system of linear equations to produce an equivalent system of linear equations.

- 1.
- 2.
- 3.

The solution(s) of a system of linear equations in more than two variables must fall into one of the following three categories:

- 1.
- 2.
- 3.

**Example 2:** Solve the system of linear equations.

$$\begin{cases} x + y + z = 3 \\ 2x - y + 3z = 16 \\ x - 2y - z = 1 \end{cases}$$

A consistent system having exactly one solution is \_\_\_\_\_ . A consistent system with infinitely many solutions is \_\_\_\_\_ .

**Example 3:** The following equivalent system is obtained during the course of Gaussian elimination. Write the solution of the system.

$$\begin{cases} x + 2y - z = 4 \\ y + 2z = 8 \\ 0 = 0 \end{cases}$$

**III. Nonsquare Systems** (Page 513)

In a square system of linear equations, the number of equations in the system is \_\_\_\_\_ the number of variables.

If a system has more variables than equations, the system cannot have a(n) \_\_\_\_\_.

**Example 4:** Solve the system of linear equations.

$$\begin{cases} x + y + z = 1 \\ x - 2y - 2z = 4 \end{cases}$$

***What you should learn***  
How to solve nonsquare systems of linear equations

**IV. Graphical Interpretation of Three-Variable Systems** (Page 514)

To sketch the graph of a plane, . . .

***What you should learn***  
How to graphically interpret three-variable systems

The graph of a system of three linear equations in three variables consists of \_\_\_\_\_ planes. When these planes intersect in a single point, the system has \_\_\_\_\_ solution(s). When the planes have no point in common, the system has \_\_\_\_\_ solution(s). When the planes intersect in a line or a plane, the system has \_\_\_\_\_ solution(s).

**V. Partial Fraction Decomposition and Other Applications**

Suppose the rational expression  $N(x)/D(x)$  is an improper fraction. Before the expression can be decomposed into partial fractions, you must . . .

***What you should learn***  
How to use systems of linear equations to write partial fraction decompositions of rational expressions and to use systems of linear equations in three or more variables to model and solve real-life problems

To decompose a proper rational expression into partial fractions, completely factor the denominator into factors of the form \_\_\_\_\_ and \_\_\_\_\_, where \_\_\_\_\_ is irreducible.

Describe how to deal with both linear factors and quadratic factors in the next step of a partial fraction decomposition.

To find the **basic equation** of a partial fraction decomposition, . . .

To solve the basic equation, . . .

**Example 5:** Write the form of the partial fraction decomposition for  $\frac{x-4}{x^2-8x+12}$ .

**Example 6:** Solve the basic equation  $5x+3 = A(x-1) + B(x+3)$  for  $A$  and  $B$ .

### Homework Assignment

Page(s)

Exercises