

Chapter 2 Functions and Their Graphs

Section 2.1

Linear equation in two variables - An equation relating two variables, x and y , whose graph is a line

Slope - The number of units the line rises (or falls) vertically for each unit of horizontal change from left to right

Slope-intercept form - A linear equation written in the form $y = mx + b$

Ratio - If the x -axis and the y -axis have the same unit of measure, then the slope has no units and is called a ratio

Rate of change - If the x -axis and the y -axis have different units of measure, then the slope is called a rate of change

Point-slope form - The equation of the line with slope m passing through the point (x_1, y_1) is

$$y - y_1 = m(x - x_1)$$

Two-point form - The equation of the line passing through points (x_1, y_1) and (x_2, y_2) is

$$y - y_1 = \frac{y_2 - y_1}{x_2 - x_1}(x - x_1)$$

General form - An equation of the form $Ax + By + C = 0$ where A and B are not both zero

Parallel - Two distinct nonvertical lines are parallel if and only if their slopes are equal. That is $m_1 = m_2$.

Perpendicular - Two distinct nonvertical lines are perpendicular if and only if their slopes are negative reciprocals of each other. That is, $m_1 = -1/m_2$.

Section 2.2

Function - A function f from a set A to a set B is a relation that assigns to each element x in the set A exactly one element y in the set B .

Domain - The set of inputs of the function f

Range - The set of all outputs for the given set of inputs of the function f

Independent variable - A variable in an equation that represents a function that can take on any value for which the function is defined

Dependent variable - A variable in an equation that represents a function whose value depends on the value of the independent variable

Function notation - The symbol, $f(x)$, read as the value of f at x or f of x , used to describe y as a function of x , where f is the name of the function and $f(x)$ is the value of the function at x

Piecewise-defined function - A function defined by two or more equations over a specified domain

Implied domain - The set of all real values for which the function is defined

Section 2.3

Graph of a function - The collection of ordered pairs $(x, f(x))$ such that x is in the domain of f

Vertical Line Test - A set of points in the coordinate plane is the graph of y as a function of x if and only if no vertical line intersects the graph at more than one point

Zeros of a function - The x -values for which $f(x) = 0$

Increasing function - A function f is increasing on an interval if, for any x_1 and x_2 in the interval, $x_1 < x_2$ implies $f(x_1) < f(x_2)$.

Decreasing function - A function f is decreasing on an interval if, for any x_1 and x_2 in the interval, $x_1 < x_2$ implies $f(x_1) > f(x_2)$

Constant function - A function f is constant on an interval if, for any x_1 and x_2 in the interval, $f(x_1) = f(x_2)$

Relative minimum - A function value $f(a)$ is called a relative minimum of f if there exists an interval (x_1, x_2) that contains a such that $x_1 < x < x_2$ implies $f(a) \leq f(x)$.

Relative maximum - A function value $f(a)$ is called a relative maximum of f if there exists an interval (x_1, x_2) that contains a such that $x_1 < x < x_2$ implies $f(a) \geq f(x)$

Linear function - A function of the form $f(x) = mx + b$

Greatest integer function - The greatest integer function is denoted by $[|x|]$ and is defined as the greatest integer less than or equal to x

Step function - A function whose graph resembles a set of stair steps

Even function - A function $y = f(x)$ is even if, for each x in the domain of f , $f(-x) = f(x)$

Odd function – A function $y = f(x)$ is odd if, for each x in the domain of f , $f(-x) = -f(x)$

Section 2.4

Vertical shift – A transformation of the graph of $y = f(x)$, represented by $h(x) = f(x) \pm c$, in which the graph is shifted upward or downward c units respectively (c is a positive real number)

Horizontal shift – A transformation of the graph of $y = f(x)$, represented by $h(x) = f(x \pm c)$, in which the graph is shifted to the left or to the right c units respectively (c is a positive real number)

Reflection – A transformation of the graph of $y = f(x)$ in which $h(x) = -f(x)$ represents a reflection in the x -axis and $h(x) = f(-x)$ represents a reflection in the y -axis

Vertical stretch – A nonrigid transformation of the graph of $y = f(x)$ represented by $y = cf(x)$ for $c > 1$. The graph appears to have been stretched vertically.

Vertical shrink – A nonrigid transformation of a graph $y = f(x)$ represented by $y = cf(x)$ for $0 < c < 1$. The graph appears to have been shrunk vertically.

Section 2.5

Arithmetic combination of functions – Two or more functions combined by the operations of addition, subtraction, multiplication, or division

Composition of functions – The composition of the function f with the function g is $(f \circ g)(x) = f(g(x))$

Section 2.6

Inverse – Let f and g be two functions. If $f(g(x)) = x$ for every x in the domain of g and $g(f(x)) = x$ for every x in the domain of f , then g is the inverse of the function f . The function g is denoted by f^{-1} .

Horizontal Line Test – A function f has an inverse if and only if no horizontal line intersects the graph of f at more than one point