

# Chapter 2 Intercepts, Zeros, and Solutions

Course Number

Instructor

Date

## Section 2.1 Modeling with Linear Equations

**Objective:** In this lesson you learned how to solve and use linear equations, including those involving fractions, and how to write and use mathematical models to solve real-life problems.

### Important Vocabulary

Define each term or concept.

**Equation**

**Extraneous**

**Mathematical modeling**

**Formulas**

**Fitting a line to data**

### I. Equations and Solutions of Equations (Pages 156–157)

To solve an equation in  $x$  means to . . .

The values of  $x$  for which the equation is true are called its

\_\_\_\_\_.

An identity equation is . . .

A conditional equation is . . .

A **linear equation in one variable  $x$**  is an equation that can be written in the standard form \_\_\_\_\_, where  $a$  and  $b$  are real numbers with  $a \neq$  \_\_\_\_\_.

### *What you should learn*

How to solve equations involving fractional expressions

**Example 1:** Solve  $5(x + 3) = 35$ .

To solve an equation involving fractional expressions, . . .

When is it possible to introduce an extraneous solution?

If a contradictory statement such as  $9 = 0$  is obtained while solving an equation, then the equation has \_\_\_\_\_.

**Example 2:** Solve: (a)  $\frac{5x}{7} = \frac{9}{14}$  (b)  $\frac{1}{x+1} + \frac{5x}{x^2-1} = \frac{4}{x-1}$

## II. Using Mathematical Models to Solve Problems

(Pages 157–159)

A good approach to mathematical modeling is to use two stages.

Begin by . . .

Then, after assigning labels to the quantities in the verbal model, . . .

When trying to construct a verbal model, it is helpful to look for a \_\_\_\_\_, that is, either an implicit or explicit statement that two algebraic expressions are equal.

**Example 3:** Describe a strategy for solving and then solve the following problem: Tuition payments make up 67% of a college student's annual income. If the student pays \$8375 for tuition in a single year, what is her annual income?

*What you should learn*  
How to write and use mathematical models to solve real-life problems

**III. Common Formulas** (Pages 160–161)

Complete the following list of common formulas for basic geometric figures.

***What you should learn***

How to use common formulas to solve real-life problems

**Perimeter/Circumference**

Square with side length  $s$ :  $P =$  \_\_\_\_\_

Rectangle with width  $w$  and length  $l$ :  $P =$  \_\_\_\_\_

Triangle with sides  $a$ ,  $b$ , and  $c$ :  $P =$  \_\_\_\_\_

Circle with radius  $r$ :  $C =$  \_\_\_\_\_

**Area**

Square with side length  $s$ :  $A =$  \_\_\_\_\_

Rectangle with width  $w$  and length  $l$ :  $A =$  \_\_\_\_\_

Triangle with base  $b$  and height  $h$ :  $A =$  \_\_\_\_\_

Circle with radius  $r$ :  $A =$  \_\_\_\_\_

**Volume**

Cube with side length  $s$ :  $V =$  \_\_\_\_\_

Rectangular solid with width  $w$ , length  $l$ , and height  $h$ :  $V =$  \_\_\_\_\_

Circular cylinder with radius  $r$  and height  $h$ :  $V =$  \_\_\_\_\_

Sphere with radius  $r$ :  $V =$  \_\_\_\_\_

Complete the following list of miscellaneous common formulas.

**Temperature**

where  $F$  = degrees Fahrenheit and  $C$  = degrees Celsius

$F =$  \_\_\_\_\_

**Simple Interest**

where  $I$  = interest,  $P$  = principal,  $r$  = annual interest rate, and  $t$  = time in years

$I =$  \_\_\_\_\_

**Compound Interest**

where  $A$  = balance,  $P$  = principal,  $r$  = annual interest rate,  
 $n$  = compoundings per year, and  $t$  = time in years

$A =$  \_\_\_\_\_

**Distance**

where  $d$  = distance traveled,  $r$  = rate, and  $t$  = time

$d =$  \_\_\_\_\_

**IV. Fitting a Line to Data** (Pages 161–163)

To fit a line to data represented in a scatter plot, . . .

***What you should learn***

How to use scatter plots and a graphing utility to find linear models for data

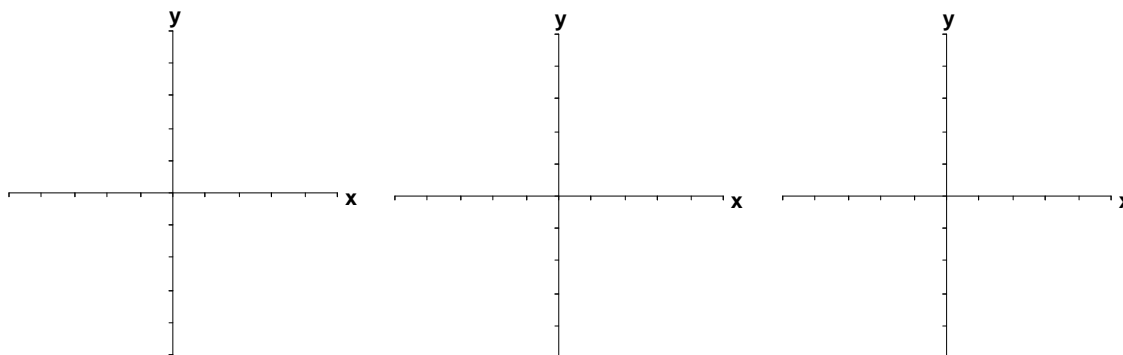
To measure how well a linear model fits the data used to find the model, . . .

The correlation coefficient  $r$  of a set of data varies between \_\_\_\_\_ and \_\_\_\_\_. The closer  $|r|$  is to 1, the better . . .

**Example 4:** The numbers of U.S. Air Force personnel  $p$  on active duty for the years 1995 through 1999 are shown in the table. Use the regression capabilities of a graphing utility to find a linear model for the data. Let  $t$  represent the year with  $t = 5$  corresponding to 1995.

Year	1995	1996	1997	1998	1999
$p$	400	389	379	363	358

(Source: U.S. Department of Defense)

**Homework Assignment**

Page(s)

Exercises