

## Section 2.3 Analyzing Graphs of Functions

**Objective:** In this lesson you learned how to analyze graphs of functions, including linear, step, and piecewise-defined functions.

Course Number

Instructor

Date

### Important Vocabulary

Define each term or concept.

**Graph of a function**

**Greatest integer function**

**Step function**

**Even function**

**Odd function**

### I. The Graph of a Function (Pages 201–202)

To find the domain of a function from its graph, . . .

#### *What you should learn*

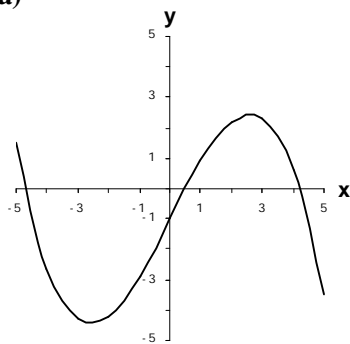
How to use the Vertical Line Test for functions

To find the range of a function from its graph, . . .

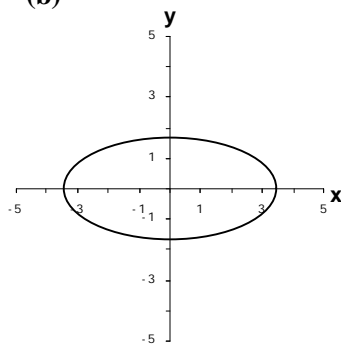
The **Vertical Line Test** for functions states . . .

**Example 1:** Decide whether each graph represents  $y$  as a function of  $x$ .

(a)



(b)



**II. Zeros of a Function** (Page 203)

If the graph of a function of  $x$  has an  $x$ -intercept at  $(a, 0)$ , then  $a$  is a \_\_\_\_\_ of the function.

The **zeros of a function**  $f$  of  $x$  are . . .

To find the zeros of a function, . . .

**Example 2:** Find the zeros of the function

$$f(x) = 4x^2 + 19x - 5.$$

***What you should learn***  
How to find the zeros of functions

**III. Increasing and Decreasing Functions** (Pages 204–205)

A function  $f$  is **increasing** on an interval if, for any  $x_1$  and  $x_2$  in the interval, . . .

A function  $f$  is **decreasing** on an interval if, for any  $x_1$  and  $x_2$  in the interval, . . .

A function  $f$  is **constant** on an interval if, for any  $x_1$  and  $x_2$  in the interval, . . .

A function value  $f(a)$  is called a **relative minimum** of  $f$  if . . .

A function value  $f(a)$  is called a **relative maximum** of  $f$  if . . .

The point at which a function changes from increasing to decreasing is a relative \_\_\_\_\_. The point at which a function changes from decreasing to increasing is a relative \_\_\_\_\_.

***What you should learn***  
How to determine intervals on which functions are increasing or decreasing

To approximate the relative minimum or maximum of a function using a graphing utility, . . .

#### IV. Linear Functions (Page 206)

A **linear function** of  $x$  is . . .

*What you should learn*  
How to identify and graph linear functions

To sketch the graph of the linear function  $f(x) = 3x - 5$ , . . .

**Example 3:** Find the linear function  $g$  for which  $g(-2) = 4$  and  $g(0) = 2$ .

#### V. Step Functions and Piecewise-Defined Functions (Page 207)

Describe the graph of the greatest integer function.

*What you should learn*  
How to identify and graph step functions and other piecewise-defined functions

**Example 4:** Let  $f(x) = \llbracket x \rrbracket$ , the greatest integer function. Find  $f(3.74)$ .

To sketch the graph of a piecewise-defined function, . . .

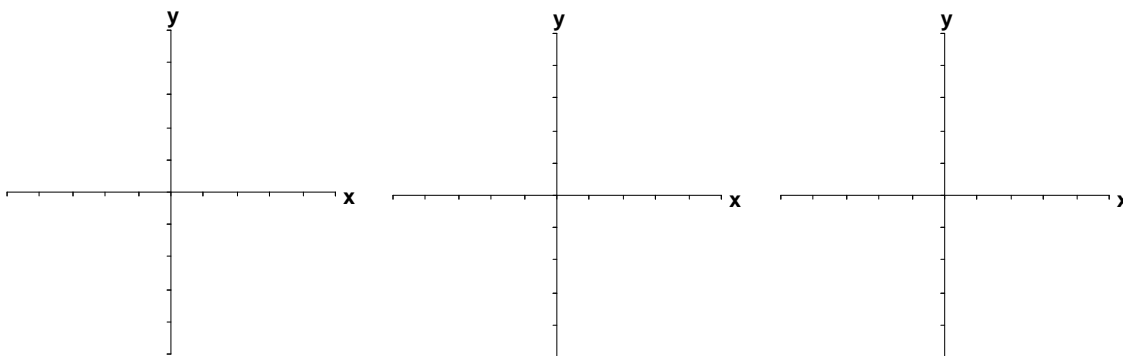
**VI. Even and Odd Functions** (Page 208)

A function whose graph is symmetric with respect to the  $y$ -axis is a(n) \_\_\_\_\_ function. A function whose graph is symmetric with respect to the origin is a(n) \_\_\_\_\_ function.

***What you should learn***  
How to identify even and odd functions

Can the graph of a nonzero function be symmetric with respect to the  $x$ -axis?

**Example 5:** Decide whether the function  $f(x) = 4x^2 - 3x + 1$  is even, odd, or neither.

**Additional notes****Homework Assignment**

Page(s)

Exercises